

Estimation of the Electron Temperature in a Li_2CO_3 Ablative Capillary Discharge

**P. Vrba^a, M.Vrbová^b,
M. Hebenstreit^c, T.Neger^c, M.Pöckl^c,
N.A.Bobrova^d, P.Sasorov^d**

^a IPP, ASCR,

Za Slovankou 3, CZ-18221 Prague 8, CR

^b CTU, FNSPE,

Břehová 7, CZ-115 19 Prague 1, CR

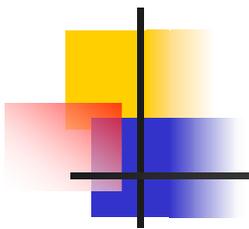
^c TUG,

Petersgasse 16, A-8010 Graz, Austria

^d ITEP,

Bolshaya Cheremuskinskaya 25, Moscow, Russia

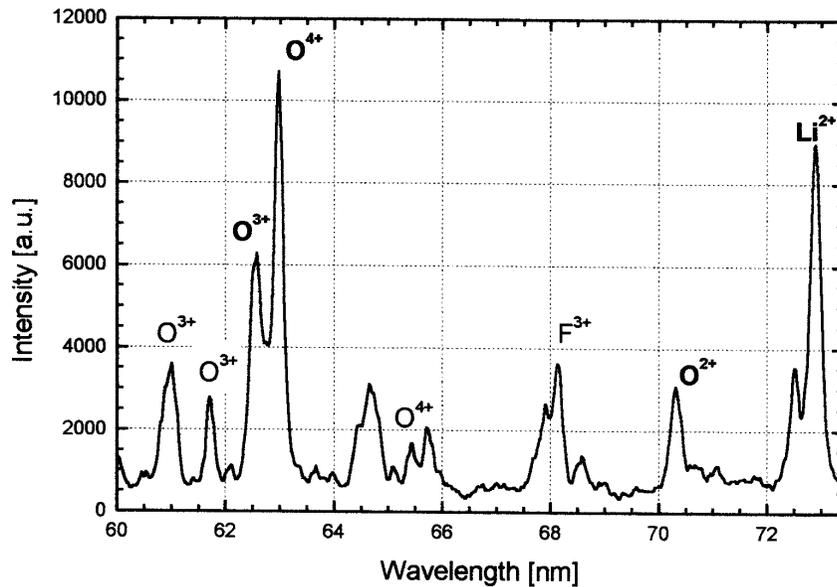
This work was supported by the program AKTION – KONTAKT under the project No. 1999-16 “Austrian – Czech contribution to the research of X-ray laser pumped by electrical discharge” and Czech Grant Agency under the project No.102/99/1559: “X-ray laser pumped by capillary electrical discharge.



Contributions:

- Measurements : TU Graz
- Data processing : CTU Prague
- Temperature estimation (IONMIX) : IPP CAS Prague
- Collisional-radiative model (CADILAC2) : TU Graz
- MHD model (NPINCH) : ITEP Moscow

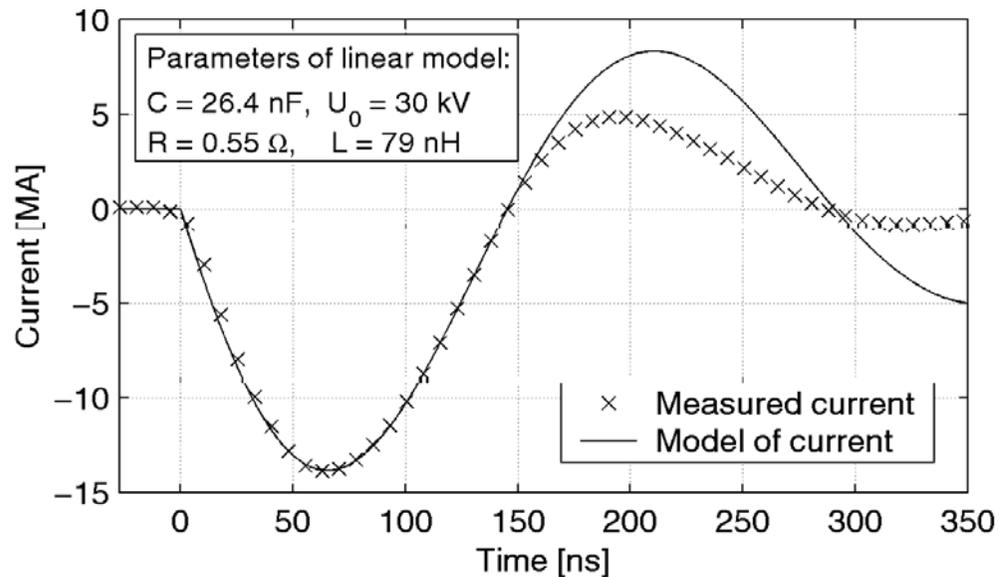
Instantaneous spectra



- Li_2CO_3 capillary discharge
- records at various delay times with gating interval 5 ns
- oxygen, lithium and fluorine ions identified

Fig. 1: Instantaneous XUV spectrum for delay time 132 ns

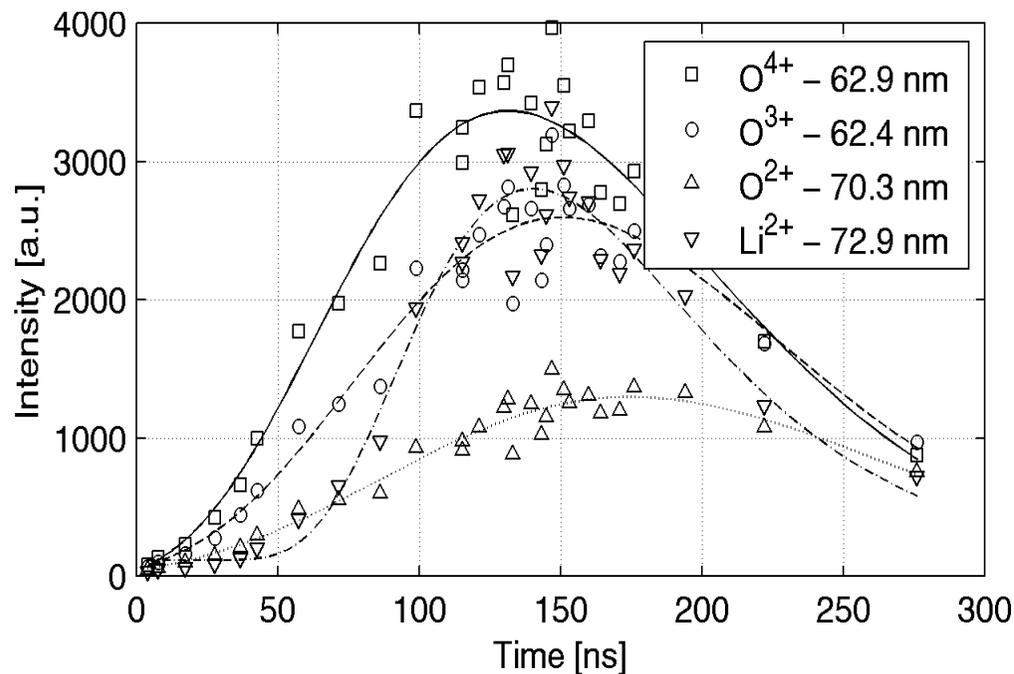
The waveform of the discharge current



- Time dependence of measured circuit current
- Approximation of under-damped serial RLC circuit

Fig. 3 : Discharge current measured and modeled

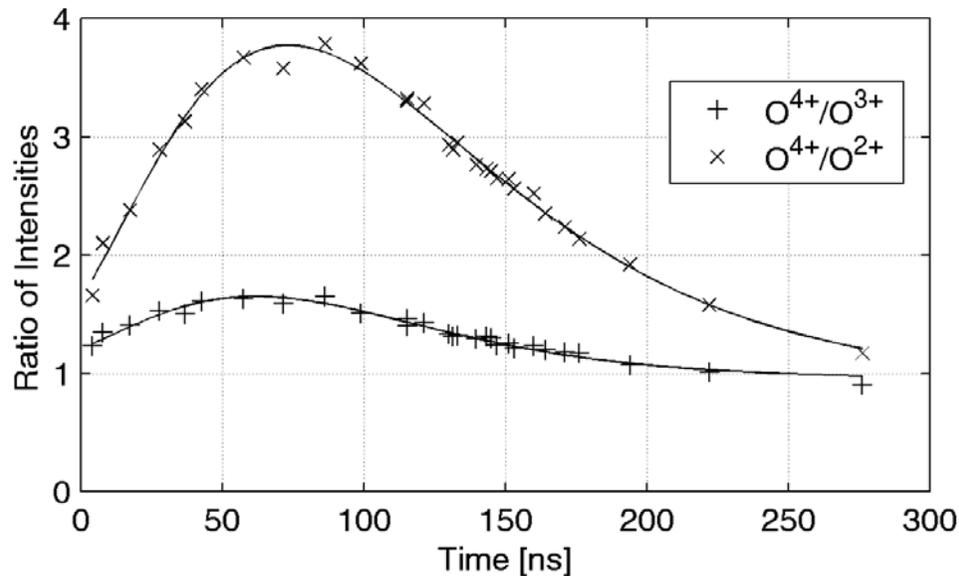
Spectra measurements in multiple shots



- The lower is the ionization state the more delayed is the peak value
- All the peaks of spectral lines are well delayed after the first discharge current maximum

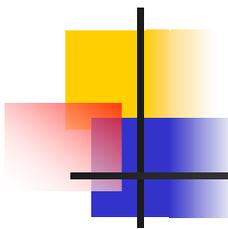
Fig. 2 : Time dependence of selected spectral lines intensities

Spectral line intensity ratios



- The ratios of the spectral line intensities of O^{4+} (63.0 nm) to O^{3+} (62.5 nm) and O^{4+} (63.0 nm) to O^{2+} (70.3 nm) show that the peak electron temperature is reached before discharge current maximum

Fig. 4 : Time dependence of ratios of intensities



Line intensity evaluation

Spectral line intensity I_{nmjk} , corresponding to the transition from the quantum state n to m of the j -th type ion of the atom k :

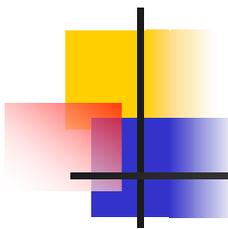
$$I_{nmjk} = h\nu_{nmjk} A_{nmjk} N_{nj}$$

$h\nu_{nmjk}$ is photon energy, A_{nmjk} the spontaneous decay rate, N_{nj} the upper level population density.

Temporal dependence of the relevant upper level populations

$$N_{nj}(t) = f_{jk}(t) f_{nj}(t) N_k,$$

$f_{jk}(t)$ and $f_{nj}(t)$ are the ionization and energy level population fractions. N_k is the number of nuclei k .



The ratio of spectral line intensities

The ratio of two spectral lines intensities

$$R = I_{nmjk} / I_{n'm'j'k'}$$

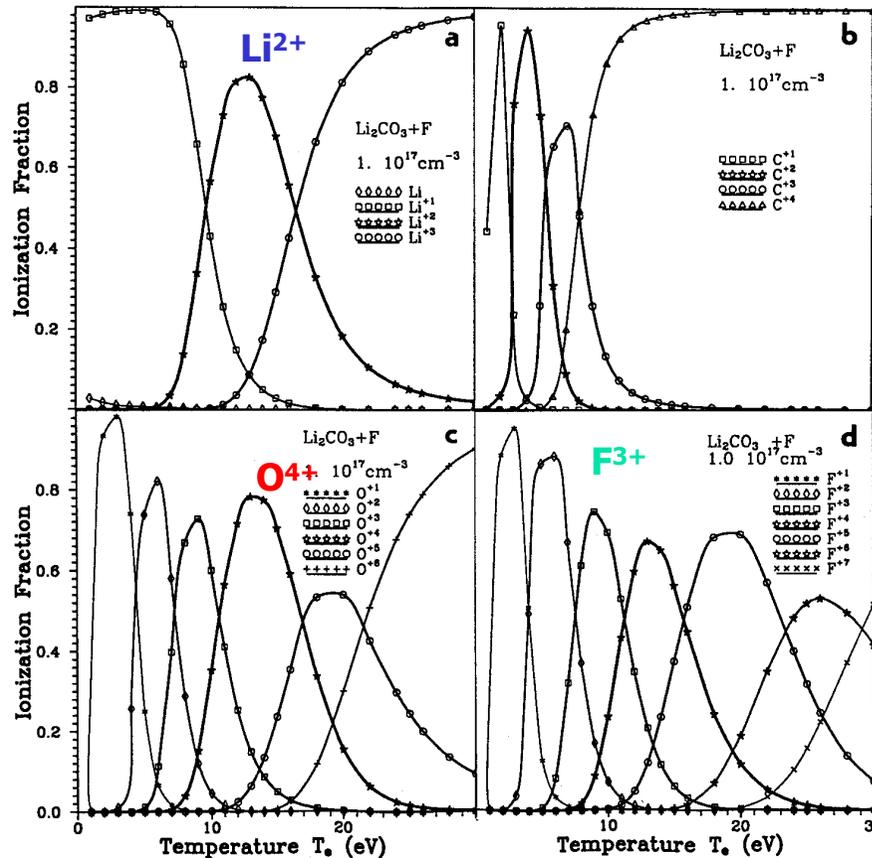
For $O^{4+}(\lambda = 62,97 \text{ nm})$ and $O^{3+}(\lambda = 62.54 \text{ nm})$, $k = k' = \text{oxygen}$,
 $j = 4$, $j' = 3$, $\nu_{nmjk} / \nu_{n'm'j'k'} = 1$ and $A_{nmjk} / A_{n'm'j'k'} = 0.449$.

If, moreover the ratio of **energy level population fractions**.
 $f_{nj} (T_e) / f_{n'j'} (T_e) = g_n / g_{n'} = 3/4$ be presumed

$$R(t) = \frac{I_{nm4,oxygen}}{I_{n'm'3,oxygen}} \cong 0.337 \frac{f_{4,oxygen}(T_e(t))}{f_{3,oxygen}(T_e(t))}$$

IONMIX code

Non-LTE ionization fractions evaluation

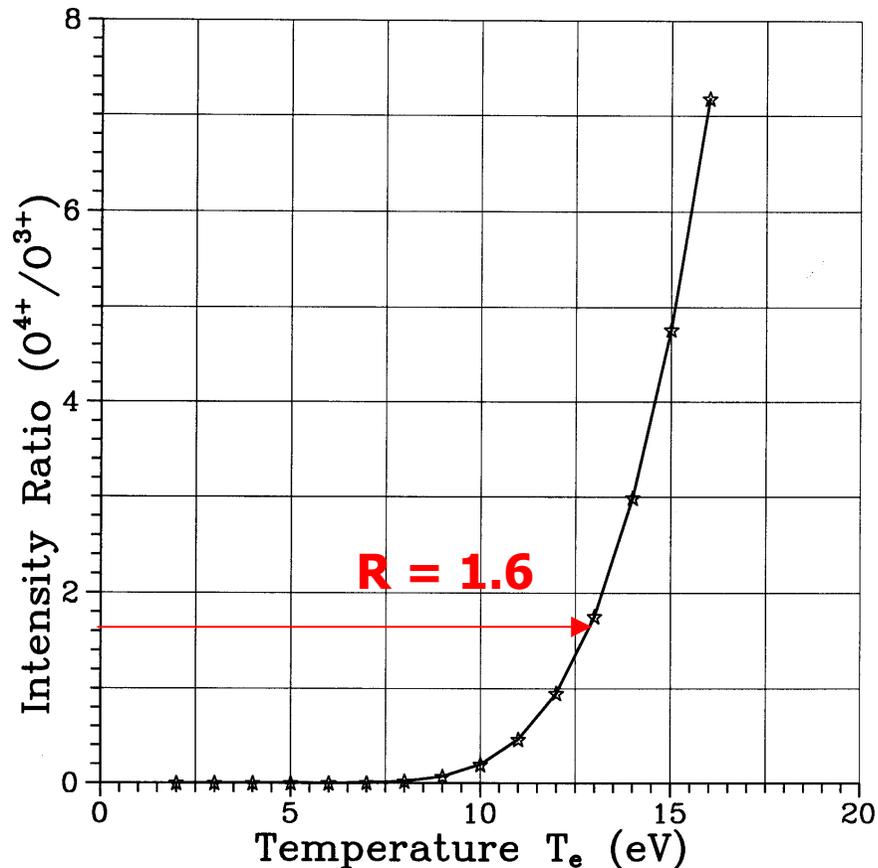


- Steady - state ionization fractions for material ablated from the Li_2CO_3 capillary wall.

- The ratio of atomic concentrations:
Li : C : O : F = 2 : 1 : 3 : 0.001

- The ionization fractions for Li, C, O, F were evaluated for $T_e = 1 \div 30 \text{ eV}$ and total density $N_{\text{tot}} = 10^{17} \text{ cm}^{-3}$.

The ratio R (predicted)

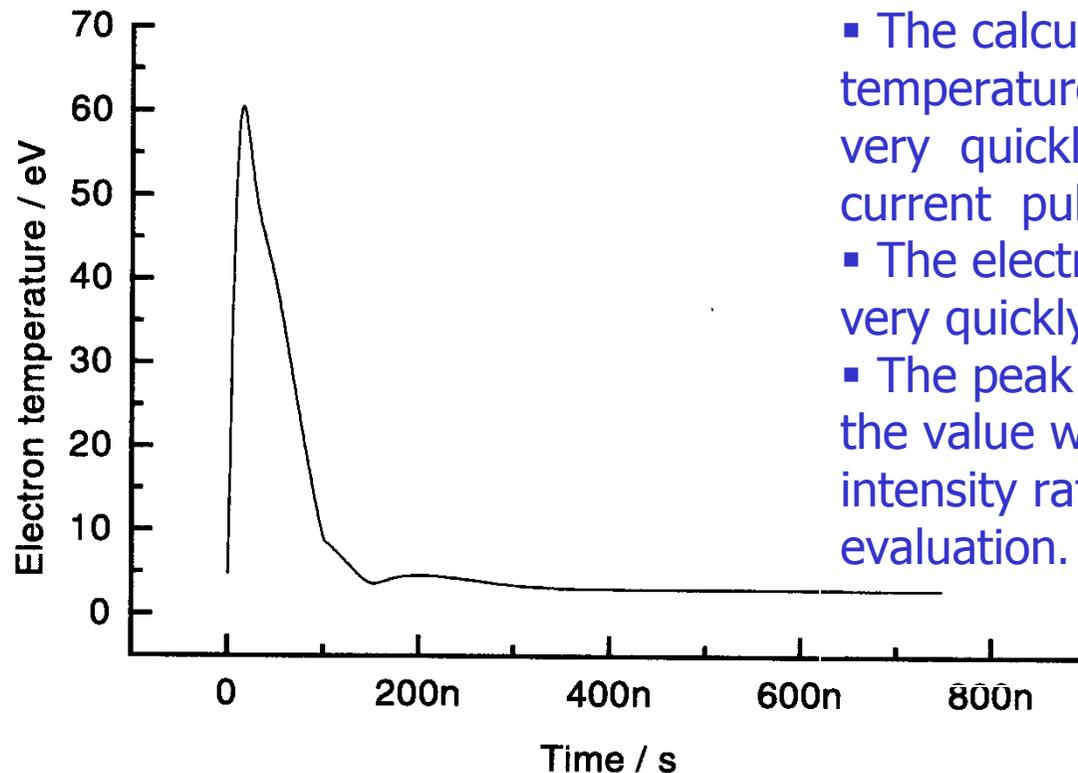


- The **ratio R is less than 1**, if the plasma electron temperature **T_e is smaller than 12 eV**.
- For temperatures **higher than 10 eV** the value of R is a rapidly **increasing function of T_e**
- If we take into account the experimental value of **$R = 1.6$** we may estimate peak electron temperature as **$T_e = 13$ eV** for **$N_{tot} = 10^{17} \text{ cm}^{-3}$**

CADILAC2 code

Zero-dimensional time dependent collisional-radiative model

- Dynamics of **lithium** atoms only
- **Circuit** equations included

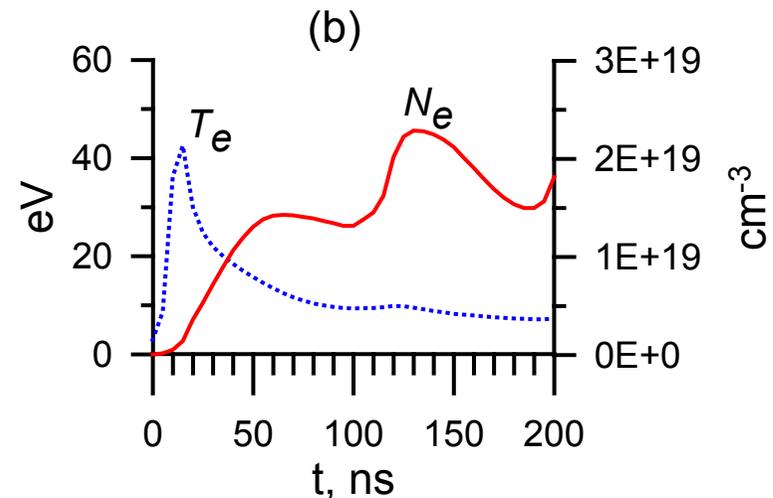
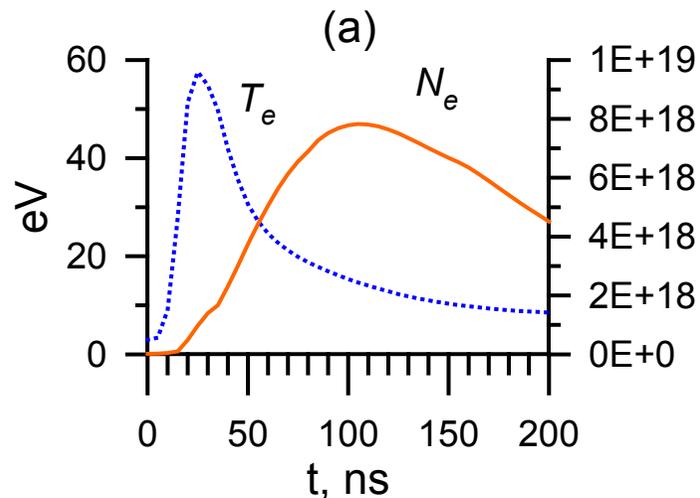


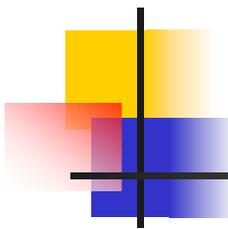
- The calculated **peak value** of electron temperature $T_e \sim \mathbf{60\ eV}$ is achieved very quickly at leading edge of the current pulse.
- The electron temperature decreases very quickly to the value about **15 eV**.
- The peak temperature is higher than the value which follows from the intensity ratio measured and **IONMIX** evaluation.

NPINCH code

Two-temperature one-fluid **MHD** model

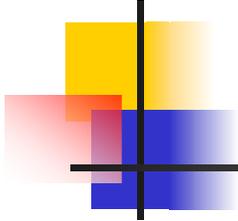
- Ablation of capillary is included
- Ionization equilibrium is presumed
- Current pulse shape follows the experiment
- The instabilities leading to **MHD turbulence** judged
- Peak plasma **electron temperature 40 ÷ 60 eV** achieved at time **15 ÷ 25 ns**
- Comparison of results **without and with MHD turbulence**, a) and b) resp.





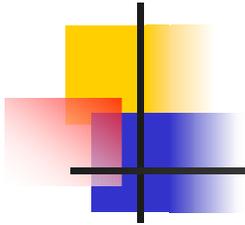
Conclusions

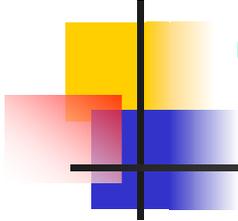
- The highest and lowest experimental values of the intensity ratio $R=3.5$ and $R=0.8$ according to the **IONMIX** code correspond to the temperatures 14 eV and 11.5 eV , respectively.
- The peak values of the electron temperature, evaluated according to the **CADILAC2** code and **NPIC- MHD** code are higher than the value which follows from the measured intensity ratio.
- The discrepancy may be explained by a **steady-state presumption**, used in the IONMIX code, and probably **not applicable for the experiment**.
- Nevertheless, at the later time ($t > 100$ ns) when the plasma is dense and temperature changes are rather slow, the **computer code predictions of temperature** as well as **the estimations based on the intensity ratio** measurements correspond each other.



References

- [1] Hebenstreit M.: *Ablative capillary discharge for use as possible XUV-laser sources Experiments and simulations*, PhD Thesis, Technische Universitaet Graz (1999)
- [2] Vrba P., Vrbova M., *Proc. XXIV ICPIG*, Warsaw, Poland (1999), Vol.1, 249-250
- [3] Pöckl M., Hebenstreit M., Neger T., Aumayr F., *J. Phys. D*, Vol.28, (1995) 47
- [4] Hebenstreit M., et al., *J. Phys.D.: Appl. Phys.*29 (1996) 1933-1940
- [5] Bobrova N. A., et al., *Plasma Physics Reports*, Vol.22 (1996), 387-402.
- [6] Vrba P., Vrbová M., *Proc. 1998 ICPP*, ECA Vol. 22 C (1998) 2856-2859
- [7] MacFarlane J.J., *Comput. Phys. Commun.* 56 (1989) 259-278
- [8] *Kelly Atomic Data*, <http://cfa-www.harvard.edu/amdata/ampddata/kelly>
- [9] *NIST Atomic Spectroscopy Database* (version 1.1) 1979-1997, <http://aeldata.phy.nist.gov>
Wiese W.L. et al.: *Atomic Transition Probabilities*, *J. Phys. Chem. Rev. Data*, Monograph 7
- [10] Huba J. D., *NRL Plasma formulary*, Naval Research Laboratory, Washington 1994



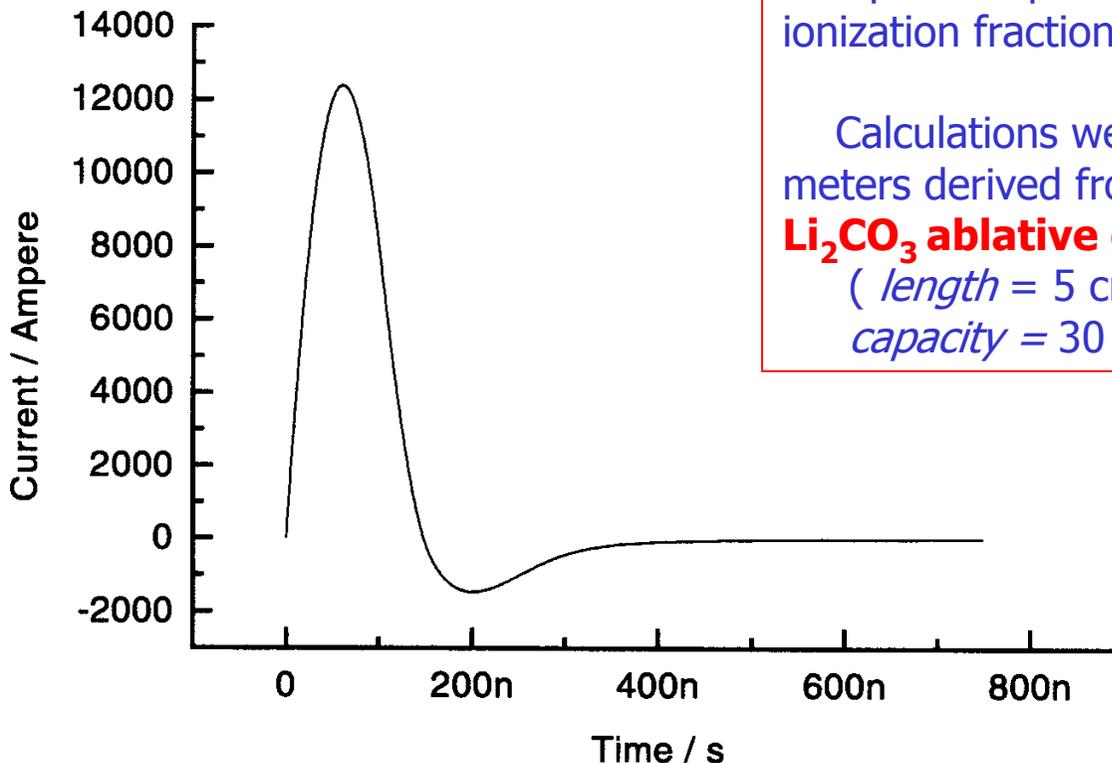


The goal Opening topic

- **Overview of the experimental data**
- **Theoretical background**
- Non-LTE ionization fractions evaluation
- Zero-dimensional collisional-radiative model
- Magnetohydrodynamic model
- **Conclusion**
- **References**

CADILAC2 code

collisional-radiative Zero-dimensional model

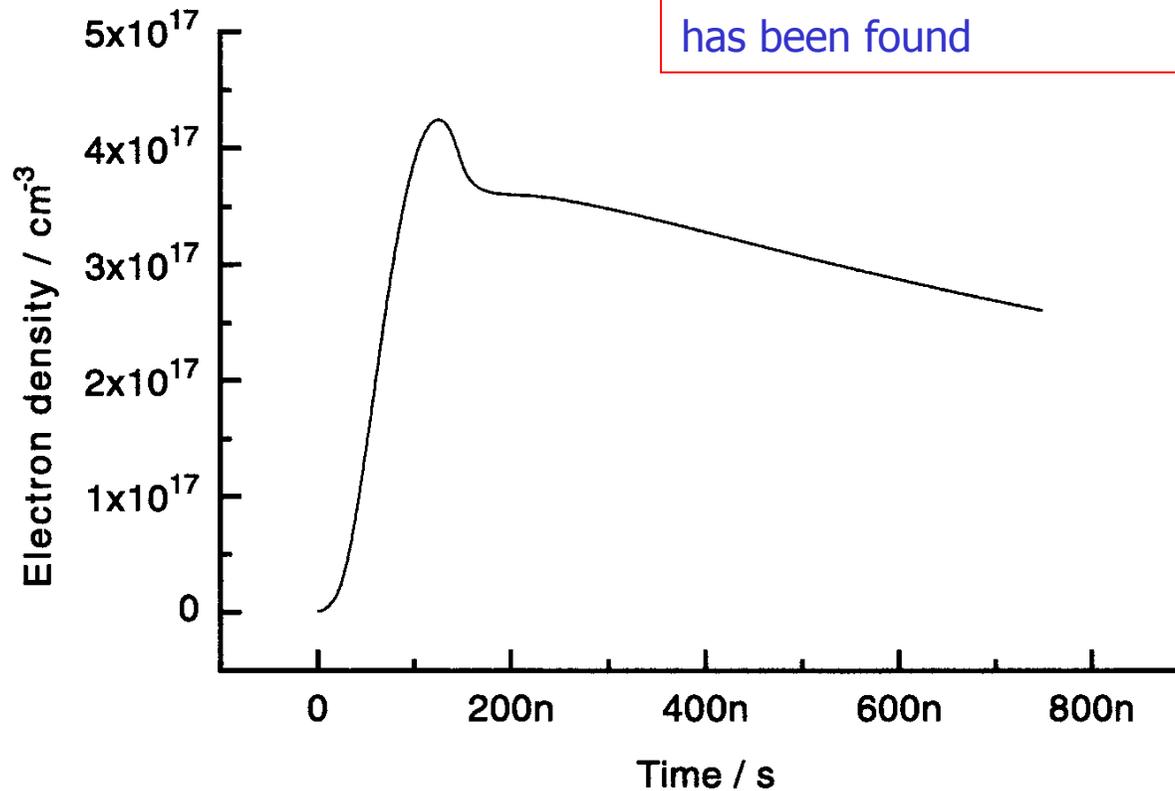


Zero-dimensional collisional-radiative model was used to calculate simultaneously the plasma parameters, population and ionization fractions.

Calculations were performed using parameters derived from actual experiments on **Li₂CO₃ ablative capillary** (*length* = 5 cm, *diameter* = 1.5 mm, *capacity* = 30 nF, *inductance* = 75 nH)

CADILAC2 code

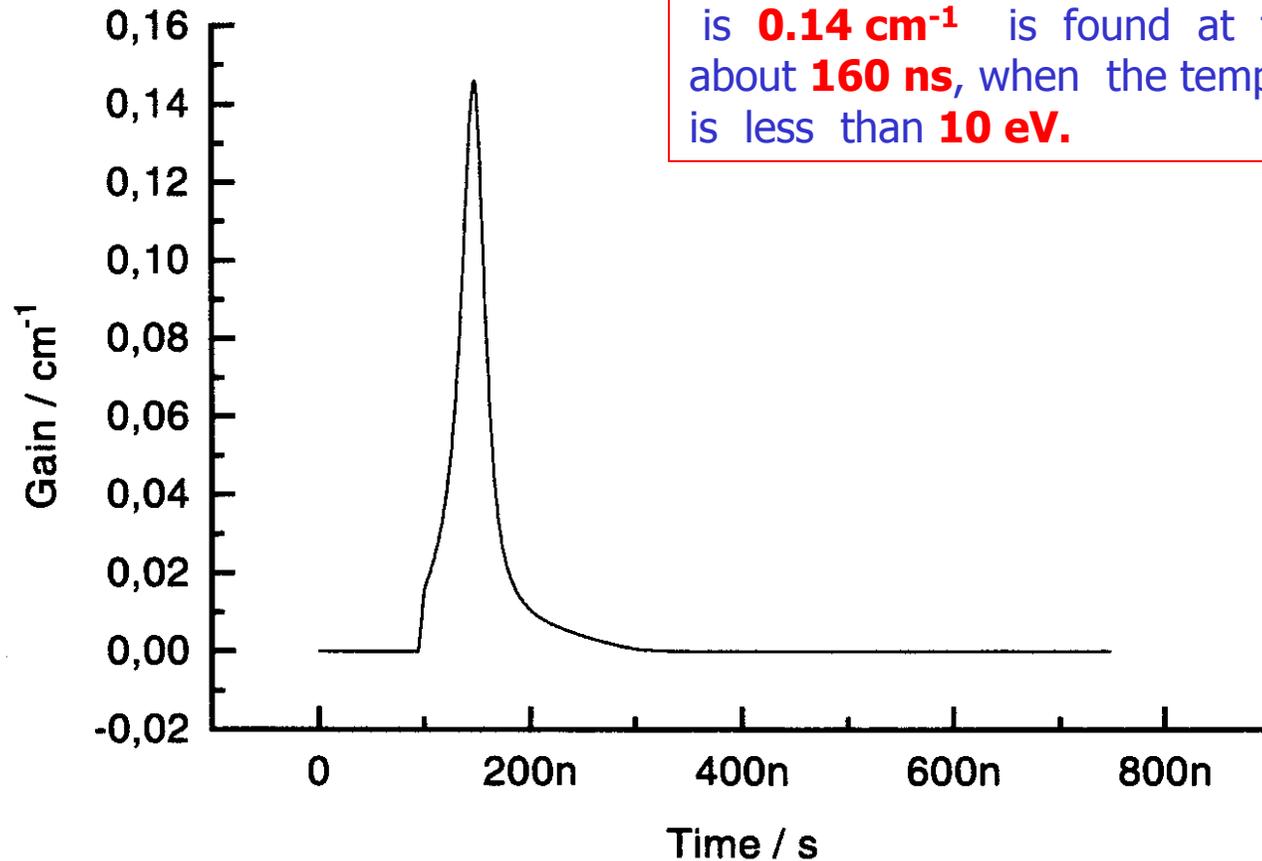
Zero-dimensional collisional-radiative model



The peak electron density at **150 ns** with a value close to **4 x 10¹⁷ cm⁻³** has been found

CADILAC2 code

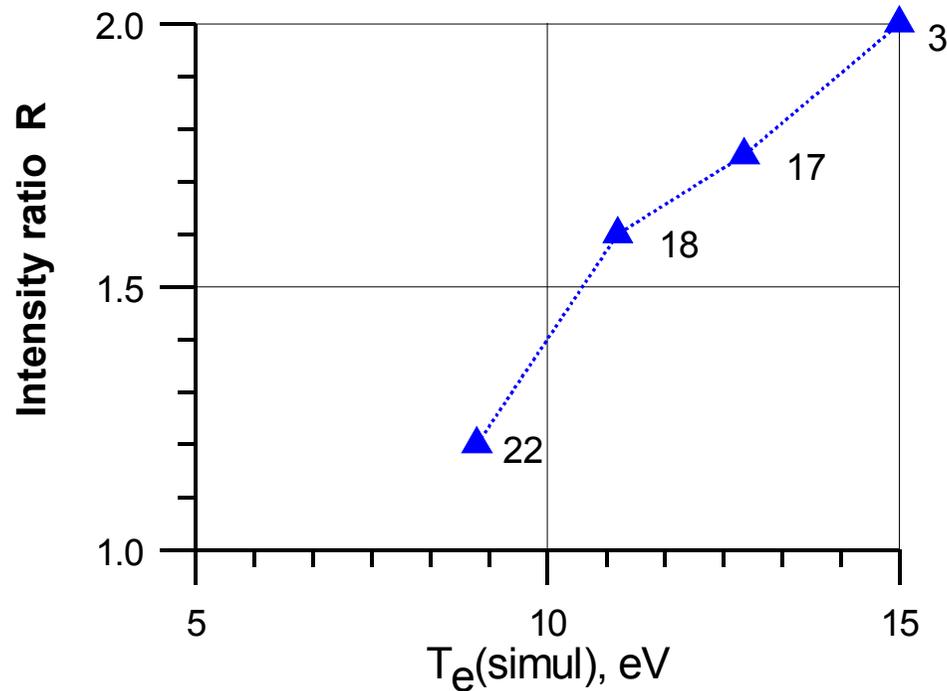
Zero-dimensional collisional-radiative model



The calculated peak value of **the gain** is **0.14 cm⁻¹** is found at the time about **160 ns**, when the temperature is less than **10 eV**.

NPINCH code

Two-temperature one-fluid **MHD** model



Correlation between simulated axial electron temperature at **$t = 100 \text{ ns}$** and values of **the ratio R** of selected spectral line intensities at the same time shows that the **electron plasma temperature** on the axis is evaluated to be equal **$9 \div 15 \text{ eV}$**